DEFLATED MINRES FOR THE GINZBURG-LANDAU PROBLEM

André Gaul

TU Berlin Str. des 17. Juni 136, 10965 Berlin, Germany e-mail: gaul@math.tu-berlin.de

Joint work with Nico Schlömer

Abstract

We consider the extreme type-II Ginzburg-Landau equations which describe phenomena of superconductivity with a nonlinear PDE model. Newton's method and discretization yield a sequence of ill-conditioned linear algebraic systems. The Jacobian operators are self-adjoint with respect to a special inner product and the linear algebraic systems can thus be solved with the preconditioned MINRES method. However, the operators become singular once the Newton iterate is close to a solution and convergence of MINRES may stagnate. Luckily, additional information can be derived from theoretical properties of the Ginzburg-Landau equation and we show how the "deflated" MINRES method can use this information to improve convergence.